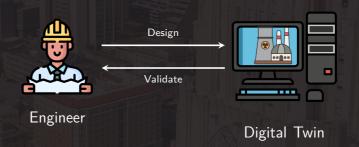
Formally Verified Autonomous Hybrid Control

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Dr. Daniel G. Cole dgcole@pitt.edu

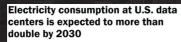
University of Pittsburgh

December 13, 2025

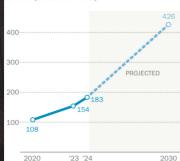




The United States stands on the precipice of a severe energy crisis



Total electricity consumption by U.S. data centers (terawatt-hours)

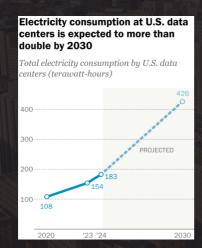


Source: Pew Research Center, Data from IEA

How much baseload power increase is this?

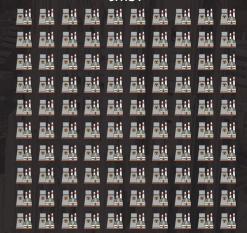


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Source: Pew Research Center, Data from IEA

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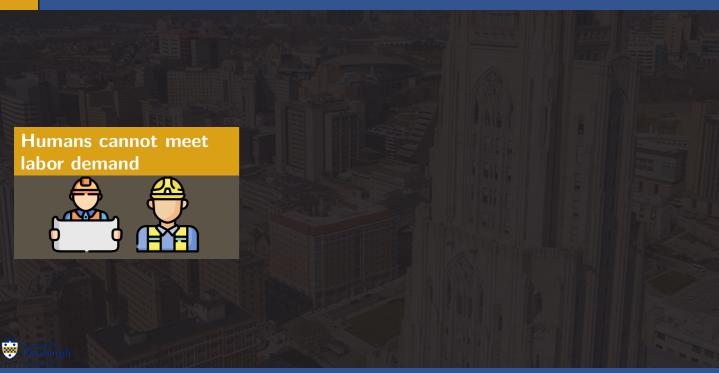
30 gigawatts!



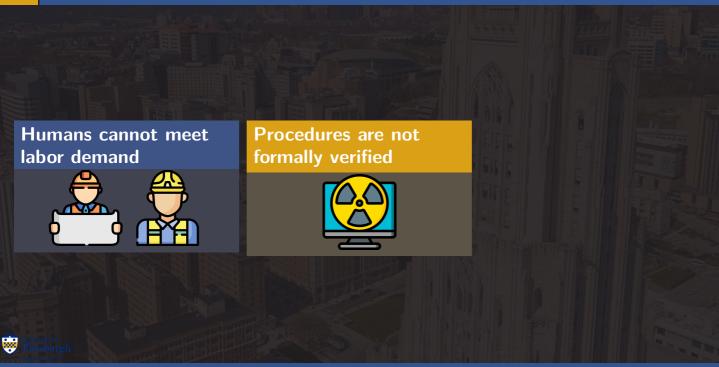
Nuclear reactors are operated with prescriptive handbooks and legacy control technologies



Human reactor operators have key limitations that limit nuclear buildout



Human reactor operators have key limitations that limit nuclear buildout



Human reactor operators have key limitations that limit nuclear buildout

Humans cannot meet labor demand





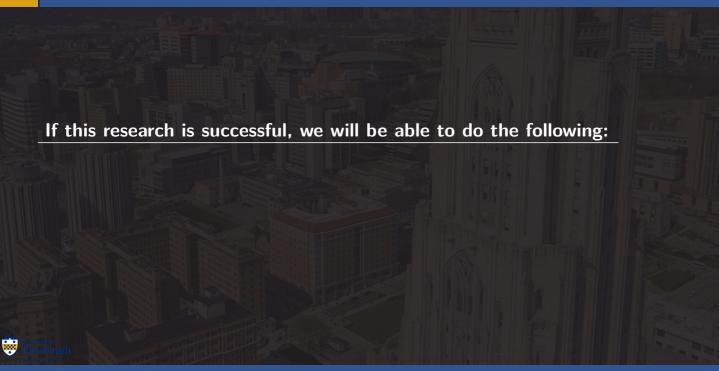
Procedures are not formally verified

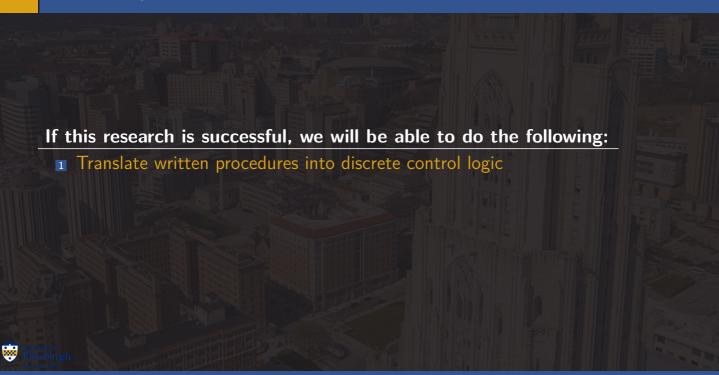


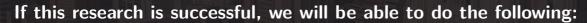
Human factors cannot be trained away











- Translate written procedures into discrete control logic
- Verify continuous control behavior across discrete mode transitions

If this research is successful, we will be able to do the following:

- Translate written procedures into discrete control logic
- Verify continuous control behavior across discrete mode transitions
- 3 Demonstrate autonomous reactor startup with verifiable safety guarantees



First, we will formalize written procedures into logical statements

APPENDIX 19-1 Plant Startup from Cold Shutdown

I. INITIAL CONDITIONS

- 1. Cold Shutdown MODE 5:
 - K_{eff} < 0.99
 - 0% power
 - T_{avg} < 200°F
- 2. Reactor Coolant System: solid.
- 3. RCS Temperature: 150 160°F.

Note:

Temperature may be less than 150°F depending upon the decay heat load of the core.

- 4. RCS Pressure: 320 400 psig.
- 5. Steam Generators: filled to wet layup (100% wide-range level indication).
- Secondary Systems: shutdown, main turbine and feedwater pump turbines on their turning gears.
- Pre-Startup Checklists: completed.





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Westinghouse Technology Systems Manual, Section 19.0 - Plant Operations

FRET Specification

INITIAL_CONDITIONS shall satisfy:

mode = MODE_5

k_eff < 0.99

power = 0

t_avg < 200

. .

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```
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    mode = MODE_5
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...</pre>
```

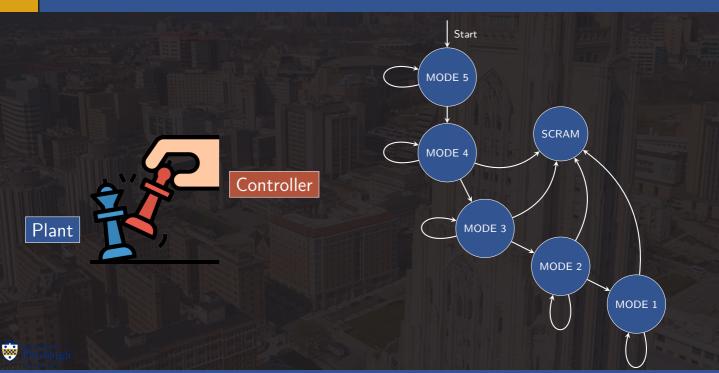
LTL Formula

```
\begin{tabular}{ll} \square & (initial $\to$ ( & mode_5_active $\land$ & $k_eff_subcritical $\land$ & $zero_power $\land$ & $temp_safe $\land$ & $\ldots$)) \\ \end{tabular}
```

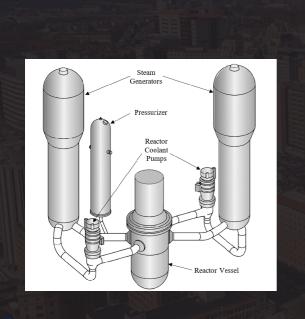


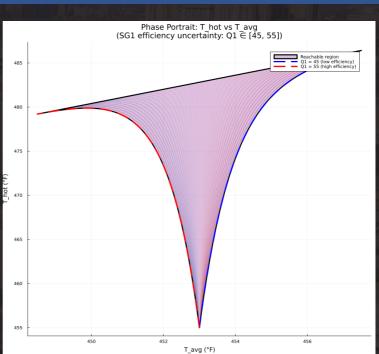
Westinghouse Technology Systems Manual, Section 19.0 - Plant Operations

Second, we will use reactive synthesis to convert the logical formulae to generate discrete automata

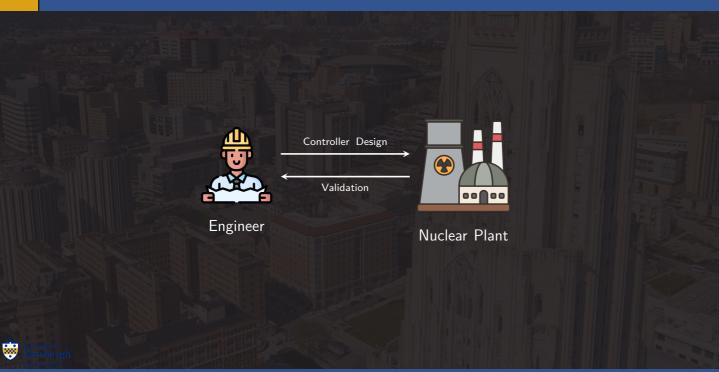


Finally, we will build continuous controllers with formal methods to ensure transitions between modes





Validating this methodology is not possible using real nuclear plants



Validating this methodology is not possible using real nuclear plants



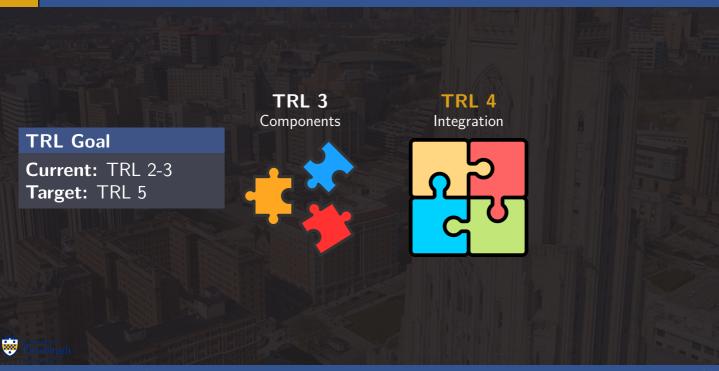
Instead, digital twins will enable controller development and validation before implementation



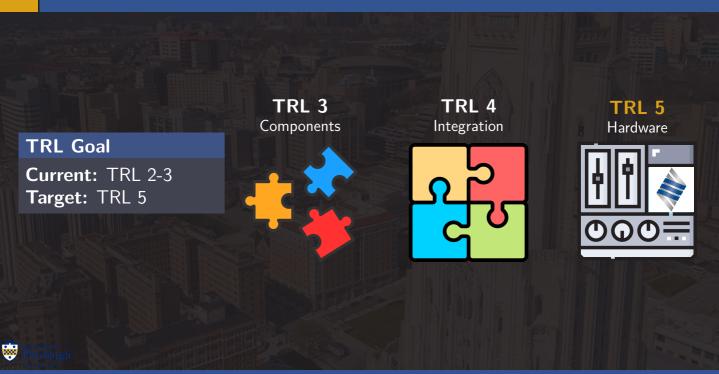
Success will be measured through Technology Readiness Level (TRL) advancement



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Reducing operations costs for new nuclear power is a billion dollar problem



Formally Verified Autonomous Hybrid Control

Enabling Economic Viability of Next-Generation Nuclear Power

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University of Pittsburgh Department of Mechanical Engineering and Materials Science

